## The

 Missing Billionaires:
## A Guide to Better Financial Decisions

Victor Haghani<br>James White

Foreword by
Emmanuel Roman, CEO of PIMCO

## Praise for The Missing Billionaires

"How much investment risk should I take? How much should I spend, and how much should I save? We all want answers to these questions, and financial economists have them, but the answers need to be translated into practical language. That's exactly why you should read this enjoyable and insightful book, to understand and apply the best thinking about risk-taking and lifetime financial planning."
-John Y. Campbell, Morton L. and Carole S. Olshan Professor of Economics at Harvard University
"Through years of dialogue with Victor and James, I have put into practice the ideas described in this book, and to great effect. They present a framework which encompasses many of the important principles I have learned through my nearly four decades of trading experience. The Missing Billionaires should be required reading at every bank, hedge fund and investment firm focused on enduring success."
-Alan Howard, Founder of Brevan Howard
"This book provides a thought-provoking, straightforward introduction to some of the most important questions in personal finance, and an engaging, non-technical description of some of the answers provided by financial economists over the past fifty years."
-Robert C. Merton, MIT Sloan School of Management Distinguished Professor of Finance, Nobel Laureate in Economic Sciences
"Haghani and White persuasively explain that to make good decisions under uncertainty, not only must we think probabilistically, but also we must apply those probabilities to the appropriate objective function. Thinking beyond the plight of the 'missing billionaires', perhaps human history would have followed a gentler and more peaceful path if our leaders had made decisions with the ideas of this book in mind."

- Philip E. Tetlock, Annenberg University Professor at the University of Pennsylvania, and co-founder of The Good Judgment Project

Cover Design: Wiley Cover Image: Jeffrey Rosenbluth Author Photos: Courtesy of the Authors

## This PDF can be found on elmwealth.com/book.

For any other inquiries, please email info@elmwealth.com.

## Preface



## 1

## Introduction: The Puzzle of the Missing Billionaires



## 2

## Befuddled Betting on a Biased Coin



Table 2.1

| Betting <br> Strategy | Bet Size | Expected <br> Outcome | Probability of <br> Hitting Max <br> Payout | Probability of <br> Going Bust |
| :--- | ---: | ---: | ---: | ---: |
| Constant Fractional | $5 \%$ | $\$ 218$ | $70 \%$ | $0 \%$ |
| Constant Fractional | $10 \%$ | $\$ 241$ | $94 \%$ | $0 \%$ |
| Constant Fractional | $20 \%$ | $\$ 237$ | $94 \%$ | $0 \%$ |
| Constant Fractional | $40 \%$ | $\$ 176$ | $70 \%$ | $0 \%$ |
| Constant Absolute | $\$ 4$ | $\$ 213$ | $59 \%$ | $7 \%$ |
| Doubling Down | $\$ 2.5$ | $\$ 72$ | $29 \%$ | $40 \%$ |



Exhibit 2.1 Summary of Coin Flipper Performance: Betting on a Coin with Disclosed Bias Toward Heads of $60 \%$, $\$ 25$ Starting Stake, $\$ 250$ Maximum Payout

## 3

## Size Matters When It's for Real



Table 3.1 Calculating Expected Payout

| Number of <br> "Heads" Flips | Number of <br> "'Tails" Flips | Probability | Ending <br> Wealth | Probability <br> $\times$ Wealth |
| :--- | :---: | ---: | ---: | ---: |
| 0 | 5 | $1.0 \%$ | $\$ 590,490$ | $\$ 6,047$ |
| 1 | 4 | $7.7 \%$ | $\$ 721,710$ | $\$ 55,427$ |
| 2 | 3 | $23.0 \%$ | $\$ 882,090$ | $\$ 203,234$ |
| 3 | 2 | $34.6 \%$ | $\$ 1,078,110$ | $\$ 372,595$ |
| 4 | 1 | $25.9 \%$ | $\$ 1,317,690$ | $\$ 341,565$ |
| 5 | 0 | $7.8 \%$ | $\$ 1,610,510$ | $\$ 125,233$ |
| Expected Payout |  | $100.0 \%$ |  | $\$ 1,104,081$ |

Table 3.2 Expected Wealth Over a Range of Betting Fractions

| Betting Fraction | Expected Wealth <br> After 25 flips |
| :---: | ---: |
| $1 \%$ | $\$ 1,051,219$ |
| $5 \%$ | $\$ 1,282,432$ |
| $10 \%$ | $\$ 1,640,606$ |
| $20 \%$ | $\$ 2,665,836$ |
| $30 \%$ | $\$ 4,291,871$ |
| $40 \%$ | $\$ 6,848,745$ |
| $50 \%$ | $\$ 10,834,706$ |
| $75 \%$ | $\$ 32,918,953$ |
| $100 \%$ | $\$ 95,396,217$ |

Table 3.3 Most Likely Wealth Over a Range of Betting Fractions

| Betting Fraction | Most Likely (Median) <br> Wealth After 25 flips |
| :---: | ---: |
| $1 \%$ | $\$ 1,049,960$ |
| $5 \%$ | $\$ 1,244,731$ |
| $10 \%$ | $\$ 1,456,516$ |
| $\mathbf{2 0 \%}$ | $\$ 1,654,316$ |
| $30 \%$ | $\$ 1,445,875$ |
| $40 \%$ | $\$ 940,661$ |
| $50 \%$ | $\$ 427,631$ |
| $75 \%$ | $\$ 4,217$ |
| $100 \%$ | $\$ 0$ |



Time

Exhibit 3.1 Illustration of volatility drag

Table 3.4 Betting "Heads" on 25 Flips of a 60/40 Biased Coin, $\$ 1 \mathrm{~mm}$ Starting Wealth

| Bet Size (\% of <br> Wealth) | $1 \%$ |  | $5 \%$ | $10 \%$ | $20 \%$ | $40 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Probability of losing <br> $80 \%$ or more of <br> starting wealth | Impossible | Impossible | $0.005 \%$ | $3 \%$ | $27 \%$ |  |
| Probability of losing <br> $50 \%$ or more of <br> starting wealth | Impossible | $0.03 \%$ | $3 \%$ | $15 \%$ | $41 \%$ |  |
| End wealth from <br> winning $13 / 25$ <br> flips | $\$ 1,008,789$ | $\$ 1,018,930$ | $\$ 975,023$ | $\$ 732,252$ | $\$ 172,774$ |  |
| End wealth from <br> winning $15 / 25$ <br> flips (median <br> outcome) | $\$ 1,049,960$ | $\$ 1,244,731$ | $\$ 1,456,516$ | $\$ 1,654,316$ | $\$ 940,661$ |  |
| Expected final <br> wealth | $\$ 1,051,219$ | $\$ 1,282,432$ | $\$ 1,640,606$ | $\$ 2,665,836$ | $\$ 6,848,475$ |  |

## Equation 3.1 Optimal Bet Size

$\gamma=\frac{\hat{k} \mu}{(\hat{k} \sigma)^{2}}$, which we can simplify and rearrange as:

$$
\hat{k}=\frac{\mu}{\gamma \sigma^{2}}
$$

## 4

## A Taste of the Merton Share



## A Taste of the Merton Share

Equation 4.1 The Merton Share
$\hat{k}=\frac{\mu}{\gamma \sigma^{2}}$ where $\mu$ is the expected excess return of the risky investment you're considering, $\sigma$ is the riskiness of that investment expressed as standard deviation of returns, and $\gamma$ is your personal degree of risk-aversion.


Exhibit 4.1 Return Versus Risk Trade-offs to Justify 60/40 Stock/Bond Allocation Using Merton Share Formula

## 5

## How Much to Invest in the Stock Market?




Exhibit 5.1 Next 10-year Realized Real Return Versus Earnings Yield at Start: US Equities 1900-2022


Exhibit 5.2 Allocation to US Equities Based on Merton Share Using Excess Earnings Yield 1997-2022


Exhibit 5.3 Excess Earnings Yield Dynamic Versus Static Asset Allocation, US Equities and 10-Year TIPS 1998-2022


Exhibit 5.4 US Equities: Earnings Yield Minus Real Yield and Real Yield 1900-2022

How Much to Invest in the Stock Market?


Exhibit 5.5 Excess Earnings Yield Dynamic Versus Static Asset Allocation: US Equities and 10-year TIPS 1900-2022


Exhibit 5.6 Excess Earnings Yield Dynamic Versus Static Asset Allocation Using Momentum as Risk Proxy: US Equities and 10-year TIPS 1900-2022

## 6

## The Mechanics of Choice



## The Mechanics of Choice



Exhibit 6.1 Concave Utility Curve and Decreasing Marginal Utility of Wealth

Table 6.1 Expected Utility of St. Petersburg Game

| Num <br> Heads <br> in a <br> Row | Probability | Payoff | Prob $\times$ <br> Payoff | Wealth | $\begin{aligned} & \mathrm{Util}(W) \\ & =\ln (W) \end{aligned}$ | Prob $\times$ Utility |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 50\% | \$2 | \$1 | \$100,002 | 11.5129 | 5.75647 |
| 4 | 3.125\% | \$32 | \$1 | \$100,032 | 11.5132 | 0.35979 |
| 10 | 0.049\% | \$2,048 | \$1 | \$102,048 | 11.5332 | 0.00563 |
| 20 | 0.000048\% | \$2.1 mm | \$1 | \$2.2 mm | 14.6027 | 0.00001 |
| 40 | 0.00000000005\% | \$2.2 tn | \$1 | \$2.2 tn | 28.4190 | 0.00000000001 |
| Sum of Probability $\times$ Payoff |  |  | Infinity |  |  |  |
| Sum of Probability $\times$ Utility |  |  |  |  |  | 11.51310 |
| Wealth Equivalent to Expected Utility: $\mathrm{e}^{11.51310}$ |  |  |  |  |  | \$100,018 |
| Starting Wealth |  |  |  |  |  | \$100,000 |
| Utility of Starting Wealth: $\ln (100,000)$ |  |  |  |  |  | 11.51293 |
| Increase in Utility from Playing |  |  |  |  |  | 0.00018 |
| Maximum Amount Willing to Pay to Play |  |  |  |  |  | \$18 |

## The Mechanics of Choice

Equation 6.1 CRRA Utility

$$
U(W)=\frac{1-W^{1-\gamma}}{\gamma-1}
$$

where $\gamma$ is the parameter that dials the level of risk-aversion and $W$ is your wealth.


Exhibit 6.2 Constant Relative Risk-aversion Utility With Different Levels of Individual Risk-aversion

Table 6.2

| Probability of heads |  |  |  | 60\% |
| :---: | :---: | :---: | :---: | :---: |
| Number of Bets |  |  |  | 25 |
| Starting Wealth (\$mm) |  |  |  | 1 |
| Bet Size |  |  |  | 10\% |
| Risk-aversion (CRRA) |  |  |  | 2 |
| Number of Winning Bets (Heads) | Probability | Profit (\$mm) | End Wealth (\$mm) | Utility of End Wealth |
| 0 | 0.00000001\% | (0.93) | 0.07 | -12.930 |
| 1 | 0.0000004\% | (0.91) | 0.09 | -10.397 |
| 2 | 0.00001\% | (0.89) | 0.11 | -8.325 |
| 3 | 0.0001\% | (0.87) | 0.13 | -6.629 |
| 4 | 0.0007\% | (0.84) | 0.16 | -5.242 |
| 5 | 0.005\% | (0.80) | 0.20 | -4.107 |
| 6 | 0.023\% | (0.76) | 0.24 | -3.179 |
| 7 | 0.092\% | (0.71) | 0.29 | -2.419 |
| 8 | 0.312\% | (0.64) | 0.36 | -1.797 |
| 9 | 0.884\% | (0.56) | 0.44 | -1.289 |
| 10 | 2.122\% | (0.47) | 0.53 | -0.873 |
| 11 | 4.341\% | (0.35) | 0.65 | -0.532 |
| 12 | 7.597\% | (0.20) | 0.80 | -0.254 |
| 13 | 11.395\% | (0.02) | 0.98 | -0.026 |
| 14 | 14.651\% | 0.19 | 1.19 | 0.161 |
| 15 | 16.116\% | 0.46 | 1.46 | 0.313 |
| 16 | 15.109\% | 0.78 | 1.78 | 0.438 |
| 17 | 11.998\% | 1.18 | 2.18 | 0.540 |
| 18 | 7.999\% | 1.66 | 2.66 | 0.624 |
| 19 | 4.420\% | 2.25 | 3.25 | 0.692 |
| 20 | 1.989\% | 2.97 | 3.97 | 0.748 |
| 21 | 0.710\% | 3.86 | 4.86 | 0.794 |
| 22 | 0.194\% | 4.93 | 5.93 | 0.831 |
| 23 | 0.038\% | 6.25 | 7.25 | 0.862 |
| 24 | 0.005\% | 7.86 | 8.86 | 0.887 |
| 25 | 0.0003\% | 9.83 | 10.83 | 0.908 |
| Expectation |  | 0.64 | 1.64 | 0.224 |

## The Mechanics of Choice



Exhibit 6.3 Expected Return and Utility over a Range of Bet Sizes For a Single Toss


Exhibit 6.4 Expected Return, RAR and Price of Risk Over Range of Bet Sizes For One Toss

Equation 6.2 Risk-Adjusted Return

$$
\text { Risk-adjusted Excess Return }=k \mu-\frac{\gamma(k \sigma)^{2}}{2}
$$

Equations 6.3 and 6.4 Restating optimal investment size and Risk-adjusted Excess Return in terms of Sharpe ratio

$$
\hat{k}=\frac{S R}{\gamma \sigma} \text { where } \hat{k} \text { is the optimal fraction of wealth to invest in the }
$$ risky asset, $S R$ is the Sharpe ratio, $\sigma$ is the risk measured in standard deviation and $\gamma$ is the investor's coefficient of risk-aversion.

And for the risk-adjusted excess return of the optimal portfolio, we get:

$$
\text { Risk-adjusted Excess Return }=\frac{S R^{2}}{2 \gamma}
$$

Table 6.3 Three Investments with Same Expected Gain and Risk but Varying Symmetry of Payoffs

|  | Positively <br> Asymmetric | Symmetric | Negatively <br> Asymmetric |
| :--- | :---: | :---: | :---: |
| Probability of Profit | $20 \%$ | $50 \%$ | $80 \%$ |
| Probability of Loss | $80 \%$ | $50 \%$ | $20 \%$ |
| Profit | $45 \%$ | $25 \%$ | $15 \%$ |
| Loss | $-5 \%$ | $-15 \%$ | $-35 \%$ |
| Expected Gain | $5 \%$ | $5 \%$ | $5 \%$ |
| Risk | $20 \%$ | $20 \%$ | $20 \%$ |
| Sharpe Ratio | 0.25 | 0.25 | 0.25 |



Exhibit 6.5 Impact of Investment Symmetry on Risk-adjusted Return


Exhibit 6.6 Comparing Wealth Outcomes for Goal-based Investing Versus Constant Risk Investing, Starting Wealth $=1$

## 7

## Criticisms of Expected Utility Decision-making

COQ MaTIUE BUASES MAKE US POOR IMVESTORS


## Criticisms of Expected Utility Decision-making



Wealth
Exhibit 7.1 Prospect Theory Versus Classical Utility Preferences

## 8

## Reminiscences of a Hedge Fund Operator



Table 8.1 Assumptions Needed for Expected Utility Analysis

## Assumptions

| Risk-free rate | $5 \%$ |
| :--- | ---: |
| Expected fund return with no incentive fee | $20 \%$ |
| Standard deviation of fund return in normal times | $15 \%$ |
| Annual probability of $90 \%$ fund loss | $0.5 \%$ |
| Management company expected return | $15 \%$ |
| Standard deviation of management company in normal times | $25 \%$ |
| Loss in value of management company if fund loses $90 \%$ | $100 \%$ |
| Fraction of total net worth in the management company | $50 \%$ |
| Victor's personal degree of CRRA risk-aversion | 2 |



Exhibit 8.1 Risk-adjusted Return as Function of Percentage of Liquid Wealth Invested in Fund

## 9

## Spending and Investing in Retirement



Table 9.1 Sam Case Study: 65 Years Old, Retired, $\$ 1 \mathrm{~mm}$ of Savings, 20 Years to Live, Can Only Invest in a Risk-Free Asset Paying 3\% After-tax and Above Inflation, Discounts Future Utility of Consumption by 2\% per Year, Has CRRA Utility with $\gamma=2$ Risk-aversion

| Age | Wealth (\$) | Risk-Free Income (\$) | Spending <br> (\%) | Spending <br> (\$) | Utility of Spending | Discounted Utility of Spending |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 65 | 1,000,000 |  |  |  |  |  |
| 66 | 965,547 | 30,000 | 6.3\% | 64,453 | 0.8448 | 0.8283 |
| 67 | 929,744 | 28,966 | 6.5\% | 64,769 | 0.8456 | 0.8128 |
| 68 | 892,551 | 27,892 | 6.8\% | 65,084 | 0.8464 | 0.7975 |
| 69 | 853,925 | 26,777 | 7.1\% | 65,403 | 0.8471 | 0.7826 |
| 70 | 813,820 | 25,618 | 7.5\% | 65,723 | 0.8478 | 0.7679 |
| 71 | 772,189 | 24,415 | 7.9\% | 66,045 | 0.8486 | 0.7535 |
| 72 | 728,986 | 23,166 | 8.3\% | 66,369 | 0.8493 | 0.7394 |
| 73 | 684,163 | 21,870 | 8.9\% | 66,693 | 0.8501 | 0.7255 |
| 74 | 637,669 | 20,525 | 9.5\% | 67,019 | 0.8508 | 0.7119 |
| 75 | 589,453 | 19,130 | 10.3\% | 67,346 | 0.8515 | 0.6985 |
| 76 | 539,462 | 17,684 | 11.1\% | 67,675 | 0.8522 | 0.6854 |
| 77 | 487,641 | 16,184 | 12.2\% | 68,005 | 0.8530 | 0.6725 |
| 78 | 433,932 | 14,629 | 13.6\% | 68,338 | 0.8537 | 0.6599 |
| 79 | 378,278 | 13,018 | 15.4\% | 68,672 | 0.8544 | 0.6475 |
| 80 | 320,617 | 11,348 | 17.7\% | 69,009 | 0.8551 | 0.6353 |
| 81 | 260,888 | 9,619 | 21.0\% | 69,347 | 0.8558 | 0.6234 |
| 82 | 199,028 | 7,827 | 25.9\% | 69,687 | 0.8565 | 0.6117 |
| 83 | 134,972 | 5,971 | 34.2\% | 70,028 | 0.8572 | 0.6002 |
| 84 | 68,652 | 4,049 | 50.6\% | 70,369 | 0.8579 | 0.5889 |
| 85 | 0 | 2,060 | 100.0\% | 70,711 | 0.8586 | 0.5778 |
| Total Lifetime Spending |  |  |  | \$1,350,745 |  |  |
| Sum of Discounted Annual Utility of Spending |  |  |  |  |  | 13.9207 |

Equation 9.1 Optimal spending to a very long horizon

$$
\hat{c}_{\infty}=r_{r a}-\frac{r_{r a}-r_{t p}}{\gamma}
$$

where
$\hat{c}_{\infty}$ is the long (infinite) horizon optimal spending rate, $r_{r a}$ is the Risk-Adjusted Return of the optimal portfolio, $r_{t p}$ is the investor's rate of time preference, and $\gamma$ is the investor's level of constant relative risk-aversion.

Equation 9.2 Optimal spending for finite horizon

$$
\hat{c}_{t}=\frac{\hat{c}_{\infty}}{1-\left(1+\hat{c}_{\infty}\right)^{-T}}
$$

Equation 9.3 Bequest function

$$
U(\text { Bequest })=\frac{b\left(1-\left(\frac{w}{b}\right)^{(1-\gamma)}\right)}{\gamma-1} .
$$

Table 9.2 Assumptions Behind Sam's Optimal Investment and Spending Policy

| Starting wealth | $\$ 1,000,000$ |
| :--- | ---: |
| Fraction in Roth IRA | $40 \%$ |
| Risk-aversion level | 2 |
| Rate of time preference | $2 \%$ |
| Average tax rate | $20 \%$ |
| Safe asset return | $4 \%$ |
| Stock market expected return | $9 \%$ |
| Stock market risk | $20 \%$ |
| Inflation Rate | $2 \%$ |

## Spending and Investing in Retirement



Exhibit 9.1 Spending and Investing Rules and Spending and Portfolio Value Statistics

Table 9.3 Sam: Fixed Spending vs Utility Optimal Variable Spending ( $60 \%$ in US Stocks, $40 \%$ in T-Bills)

|  | $\begin{array}{r} \text { S\&P } 500 \\ \text { Return } \end{array}$ | Wealth 5\% Spending Rule | Fixed <br> Real <br> Spend per 5\% <br> Rule | Wealth <br> Utility <br> Opt Plan | Utility Opt <br> Spend |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1999 |  | \$1,000,000 |  | \$1,000,000 |  |  |
| 2000 | -9.7\% | \$916,247 | \$50,000 | \$923,019 | 4.3\% | \$42,979 |
| 2001 | -11.8\% | \$809,334 | \$51,693 | \$826,041 | 4.4\% | \$40,618 |
| 2002 | -21.6\% | \$662,400 | \$52,496 | \$690,400 | 4.5\% | \$37,211 |
| 2003 | 28.2\% | \$713,782 | \$53,743 | \$772,316 | 4.6\% | \$31,831 |
| 2004 | 10.7\% | \$707,082 | \$54,753 | \$789,537 | 4.7\% | \$36,436 |
| 2005 | 4.8\% | \$679,762 | \$56,536 | \$785,175 | 4.8\% | \$38,108 |
| 2006 | 15.8\% | \$692,503 | \$58,467 | \$831,956 | 4.9\% | \$38,765 |
| 2007 | 5.1\% | \$660,027 | \$59,952 | \$824,263 | 5.0\% | \$42,007 |
| 2008 | -36.8\% | \$465,904 | \$62,399 | \$609,412 | 5.2\% | \$42,555 |
| 2009 | 26.4\% | \$467,423 | \$62,456 | \$668,782 | 5.3\% | \$32,164 |
| 2010 | 15.1\% | \$439,705 | \$64,156 | \$689,873 | 5.4\% | \$36,078 |
| 2011 | 1.9\% | \$378,901 | \$65,116 | \$659,343 | 5.5\% | \$38,032 |
| 2012 | 16.0\% | \$341,855 | \$67,045 | \$682,056 | 5.6\% | \$37,139 |
| 2013 | 32.3\% | \$326,729 | \$68,212 | \$767,510 | 5.8\% | \$39,247 |
| 2014 | 13.5\% | \$278,446 | \$69,236 | \$781,187 | 5.9\% | \$45,108 |
| 2015 | 1.2\% | \$210,632 | \$69,760 | \$741,150 | 6.0\% | \$46,885 |
| 2016 | 12.0\% | \$151,759 | \$70,269 | \$752,218 | 6.1\% | \$45,417 |
| 2017 | 21.7\% | \$90,889 | \$71,727 | \$800,819 | 6.3\% | \$47,056 |
| 2018 | -4.6\% | \$17,272 | \$73,239 | \$733,649 | 6.4\% | \$51,131 |
| 2019 | 31.2\% | \$0 | \$17,272 | \$814,514 | 6.5\% | \$47,802 |
| 2020 | 18.3\% | \$0 | \$0 | \$844,134 | 6.6\% | \$54,149 |
| 2021 | 28.7\% | \$0 | \$0 | \$922,212 | 6.8\% | \$57,249 |
| 2022 | -18.2\% | \$0 | \$0 | \$884,418 | 6.9\% | \$56,344 |
| Avg Equity <br> Return | 7.84\% |  |  |  |  |  |
| Avg T-Bill <br> Return | 1.36\% |  |  |  |  |  |
| Avg Inflation | 2.51\% |  |  |  |  |  |
| Total Spending |  |  | \$1,198,528 |  |  | \$984,314 |
| Total Spending + Wealth at End |  |  | \$1,198,528 |  |  | \$1,868,733 |

## 10

## Spending Like You'll Live Forever



Table 10.1 Investment Environment and Policy Assumptions

| Long-term risk-free real rate | $0 \%$ |
| :--- | ---: |
| Expected real return on a well-chosen mix | $6 \%$ |
| of public and private market risky assets |  |
| Risky assets annual variability of returns | $18 \%$ |
|  | $90 \%$ in risky assets |
| Endowment asset allocation | $10 \%$ in risk-free assets |
| Endowment expected return | $5.4 \%$ |



Exhibit 10.1 Policy 1: Spend a Fixed Annual Amount Equal to the Expected Simple Return of the Portfolio


Exhibit 10.2 Policy 2: Spend a Fixed Annual Percentage of the Endowment Value Equal to the Expected Return of the Portfolio


Exhibit 10.3 Policy 3: Spend a Fixed Annual Percentage of the Endowment Value Equal to the Expected Compound Return of the Portfolio

Table 10.2 Comparing Spending Rules: Size of Endowment Needed to Generate Equal Welfare Over 100 Years Under Different Spending Policies

| Rule 1: Spend | Rule 2: Spend <br> 55.40 per annum | Rule 3: Spend <br> 4.1\% per annum |
| :--- | ---: | ---: |
| $\$ 172$ | $\$ 152$ | $\$ 100$ |



Exhibit 10.4 Median Spending Under Optimal and Sustainable Spending
Policies

## 11

## Spending Like You Won't Live Forever




Exhibit 11.1 Longevity Probabilities for 65-year-old Female From US Social Security Mortality Tables (2015)


Exhibit 11.2 Comparing Self-Managed Versus Annuity Annual Expenditure for Sam Age 65

## 12

## Measuring the Fabric of Felicity



Measuring the Fabric of Felicity


Exhibit 12.1 Survey Responses


## Spending

Exhibit 12.2 Utility Curve With Higher Risk-aversion Below
Subsistence Level

## Measuring the Fabric of Felicity



Exhibit 12.3 Friedman-Savage Utility Curve Incorporating Intermediate Range of Risk-seeking

## 13

## Human Capital




Exhibit 13.1 Typical Lifetime Earning and Spending Pattern

## 14

# Into the Weeds: <br> Characteristics of Major Asset Classes 




Exhibit 14.1 Stock Price Probability Distribution: 10\% per Annum Expected Excess Return, 75\% Annual Standard Deviation, 5-year Horizon

## 15

No Place to Hide: Investing in a World with No Safe Asset



Exhibit 15.1 US T-bills Are Far from Risk-free: Constant Standard of Living 30-year Annuity in 1997 Dollars (1997-2022)


## 16

## What About Options?



Table 16.1 Base-Case Investor Assumptions

| Equities Expected Arithmetic Return | $5 \%$ |
| :--- | :---: |
| Equities Annual Volatility | $20 \%$ |
| Safe Asset Return | $0 \%$ |
| Investor CRRA Risk-Aversion | 2 |



Exhibit 16.1 Contribution of Puts Versus Portfolio Leverage: Increase in Risk-adjusted Return for Optimal Portfolios With Versus Without Put Options

## 17

## Tax Matters



Table 17.1 Assumptions for Capital Gains Tax Realization Decision

| Current Equity Allocation | $75 \%$ | Horizon (years) | 20 |
| :--- | ---: | :--- | ---: |
| Unrealized Gains \% of Portfolio | $50 \%$ | Risk-free Rate | $3 \%$ |
| Capital Gains Tax Rate Today | $30 \%$ | Stock Market Expected Return | $6 \%$ |
| Capital Gains Tax Rate at Horizon | $30 \%$ | Stock Market Risk | $20 \%$ |
| Tax on Equity Dividends | $30 \%$ | Stock Market Dividend Rate | $2 \%$ |
| Tax on Interest | $50 \%$ | Investor Risk-Aversion (CRRA) | 2 |
| Future Value of Capital Losses |  | 0 |  |

*If a capital loss arises at the horizon, for simplicity we assume the investor derives no future value from this loss as a carryforward.


Exhibit 17.1 How Much Appreciated Asset to Sell?


Exhibit 17.2 Optimal Equity Allocation With and Without Taxes for Different Horizons

## 18

## Risk Versus Uncertainty



## Risk Versus Uncertainty



Exhibit 18.1 Multi-Round Ellsberg Experiment: \$100 Prize for Choosing Red Ball, Choosing 100 Rounds from Urn A or from Urn B, Urn A: 50 Red and 50 Black Balls, Urn B: 100 Balls, Uniformly Likely Combinations of 0-100 Red and Rest Black

Table 18.1

| Horizon | Asset A |  |  |  | Asset B |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{r} \text { Opt } \\ \text { Alloc } \end{array}$ | Return of Exp Price |  | Vol | Opt <br> Alloc | Return of Exp Price |  | Vol |
| 1 y | 62.5\% | 5.0\% | 3.0\% | 20.0\% | 62.2\% | 5.0\% | 3.0\% | 20.1\% |
| 5 y | 62.5\% | 5.0\% | 3.0\% | 20.0\% | 60.9\% | 5.1\% | 3.0\% | 20.5\% |
| 10 y | 62.5\% | 5.0\% | 3.0\% | 20.0\% | 59.5\% | 5.2\% | 3.0\% | 21.0\% |
| 30 y | 62.5\% | 5.0\% | 3.0\% | 20.0\% | 54.5\% | 5.6\% | 3.0\% | 22.8\% |
| 100 y | 62.5\% | 5.0\% | 3.0\% | 20.0\% | 44.5\% | 6.3\% | 3.0\% | 28.2\% |



Exhibit 18.2 Less than 1\% Difference in Optimal Allocation to Equities Under These Four Different Probability Distributions of Stock Price Returns, All with the Same Expected Return (5\%) and Risk (20\%) for Investor with Risk-aversion of 2

## 19

## How Can a Great Lottery Be a Bad Bet?



## 20

## The Equity Risk Premium Puzzle



## The Equity Risk Premium Puzzle

Equations 20.1, 20.2 and 20.3 Equilibria in fish economy

$$
\begin{aligned}
& r_{\text {bond }}=\delta+\gamma\left(\mu-(1+\gamma) \frac{\sigma^{2}}{2}\right) \\
& r_{\text {stock }}=\delta+\gamma\left(\mu-(\gamma-1) \frac{\sigma^{2}}{2}\right)
\end{aligned}
$$

Equity Risk Premium $=r_{\text {stock }}-r_{\text {bond }}=\gamma \sigma^{2}$
$\mu$ is the expected growth of the economy, $\sigma$ is the variability in that growth, $\gamma$ is the coefficient of risk-aversion, and $\delta$ is the time preference of the representative individual.

## 21

## The Perpetuity Paradox and Negative Interest Rates



## The Perpetuity Paradox and Negative Interest Rates



Exhibit 21.1 Price of 100-year, 1,000-year and Perpetual Annuities: Present Value of $\$ 1$ per Year

## 22

## When Less Is More




Exhibit 22.1 How Much to Wager on a Digital Asset as Payout Becomes More Favorable: Investor with CRRA Utility Risk-aversion 2

## 23

## The Costanza Trade




Exhibit 23.1 3x Leveraged Long ETF Predicted Return Versus Unleveraged Index Return: George's 1.25-year horizon. S\&P 500 Volatility $=28 \%$

Table 23.1

| Leverage Ratio | Compound Return per Annum (nominal) | Risk per Annum | End Value of $\$ 1$ | Maximum Peak-toTrough Drawdown |
| :---: | :---: | :---: | :---: | :---: |
| 0.50 | 7.1\% | 9.5\% | \$682 | -55\% |
| 0.75 | 8.6\% | 14.2\% | \$2,437 | -73\% |
| 1.00 | 9.8\% | 19.0\% | \$7,059 | -84\% |
| 1.50 | 11.0\% | 28.5\% | \$19,503 | -95\% |
| 2.00 | 11.1\% | 38.1\% | \$22,882 | -98.5\% |
| 3.00 | 8.5\% | 57.7\% | \$2,233 | -99.9\% |
| 4.00 | 1.7\% | 78.4\% | \$4.79 | -99.999\% |
| 5.00 | -infinity | 170.7\% | \$0.00 | -100.000\% |

The table assumes daily rebalancing, no transaction costs, no fees, no market impact, borrowing at 3-month T-bill rates $+1 \%$. Attentive readers will notice the maximum loss of $84 \%$ in the case of the 1.0 leverage ratio, which is smaller than the near $90 \%$ loss we have referred to previously. The difference is that here we are measuring total returns including dividends, while the near $90 \%$ loss is exclusive of dividends.

## 24

## Conclusion: $U$ and Your Wealth



# Bonus Chapter: Liar's Poker and Learning to Bet Smart 




## A Few Rules of Thumb

Constant relative risk-aversion (CRRA) utility

$$
\begin{aligned}
& U(W)=\frac{1-W^{1-\gamma}}{\gamma-1} \text { for } \gamma \neq 1 \\
& U(W)=\ln (W) \text { for } \gamma=1
\end{aligned}
$$

Merton share for asset allocation, risk-taking, and bet-sizing

$$
\hat{k}=\frac{\mu}{\gamma \sigma^{2}}
$$

$\gamma=1$ is equivalent to the Kelly criterion
Risk-adjusted Return $\left(r_{r a}\right)$, a.k.a., Certainty-equivalent Return

$$
\begin{aligned}
r_{r a} & =r_{r f}+\frac{\hat{k} \mu}{2} \text { for optimal } \hat{k}, \text { or more generally } \\
r_{r a} & =r_{f f}+k\left(\mu-\frac{k \gamma \sigma^{2}}{2}\right) \\
\text { Cost of Risk } & =\frac{\gamma(k \sigma)^{2}}{2}
\end{aligned}
$$

Optimal spending
$\hat{c}_{\infty}=r_{r a}-\frac{r_{r a}-r_{t p}}{\gamma}$ for infinite life and
$\hat{c}_{t}=\frac{\hat{c}_{\infty}}{1-\left(1+\hat{c}_{\infty}\right)^{-T}}$ for finite life $T$, i.e., wealth annuitized over
$T$ at rate $\hat{c}_{\infty}$. For $\hat{c}_{\infty}=0, \hat{c}_{\mathrm{t}}=\frac{1}{T}$.

## A Few Rules of Thumb

Symbols and assumptions

- $W$ is wealth
- $c$ is consumption as a fraction of wealth per unit time
- $k$ is the fraction of wealth allocated to the risky asset
- $k$ is the optimal allocation
- $\gamma$ is coefficient of risk-aversion in CRRA utility (for wealthy investors above subsistence typically $2-3$, the higher the more risk-averse)
- $r_{f}$ is safe asset return (for long-term US investors, real yield of long-term TIPS)
- $r_{t p}$ is the investor's rate of time preference (typical values $0 \%-4 \%$ )
- $\mu$ is expected excess return of risky asset above safe asset return (for broad equity markets typically $3 \%-6 \%$, expressed as arithmetic expected return)
- $\sigma$ is the variability of risky asset expressed as standard deviation of returns (for broad equity markets typically 15\%-20\%)


## About the Authors

Victor Haghani has spent four decades actively involved in markets and financial innovation. He started his career in 1984 at Salomon Brothers in bond research. He moved to the trading floor in 1986 and shortly after became a managing director in the bond arbitrage group run by John Meriwether. In 1993, Victor was a cofounding partner of Long-Term Capital Management (LTCM). He established and co-ran its London office. His participation in the failure of LTCM was a life-changing experience that led him to question and revise much of the way he thought about the economy, markets, and investing.

Through a careful study of the academic literature on investing and many thought-provoking discussions with friends, colleagues, and investors of all backgrounds, Victor concluded that savers can and should do much better. He founded Elm Wealth in 2011 to help investors, including his own family, manage their savings in a disciplined, research-based, cost-effective manner and to capture the long-term returns they ought to earn.

In his 2013 TEDx talk, Where Are All the Billionaires and Why Should We Care?, Victor shared his perspective on the synthesis of active and passive investing, which forms the basis of the Dynamic Index Investing ${ }^{\circledR}$ approach offered by Elm Wealth. Over the years, Victor became fascinated with the challenge of making good decisions on broader questions about wealth and personal finances, including sound spending policies, tax decisions, and retirement choices.

Victor was born in New York City in 1962 and grew up in New York, Pennsylvania, Tehran, and London. As an adult, he has resided in New York City and London and, more recently, has been based in Jackson Hole, Wyoming. Victor graduated from the London School of Economics (LSE) in 1984 with a B.Sc. (economics). He has been a prolific contributor to the academic and practitioner finance literature.

Victor has been involved in a variety of other activities, including research and lecturing at the LSE, where he was a senior research associate in the Financial Markets Group, as well as consulting and board assignments and acting as a "name" in the Lloyd's of London insurance market. He loves the outdoors and is an avid skier, hiker, and fisherman and enjoys taking long walks with his dog Milo. He has always been fascinated by airplanes, flying model ones as a boy and full-size ones as an adult.

James White has spent two decades working in finance, covering the gamut of quantitative research, market-making, hedge fund investing, private equity investing, and wealth management. He has been the chief executive officer (CEO) of Elm Wealth since 2018, working with Victor to help friends, family, and clients sensibly and efficiently invest their wealth. After meeting through a mutual friend, James and Victor began working on research and writing together, sharing ideas, and collaborating regularly. After James built the next generation of Elm's portfolio management systems, he and Victor were talking and working together every day so joining Elm as the CEO just seemed natural.

Since then James has moved to Philadelphia to establish Elm's headquarters and has seen the business grow to serve hundreds of families and manage around $\$ 1.5$ billion of their assets. He splits his time between working with clients, continuing to develop and improve Elm's systems, and research and writing.

After studying math at the $u$ niversity of Chicago, James lived and worked all over the world, first for Nationsbank/Cr T and Bank of America, then for Citadel Investment Group, then as a partner at PAC Partners, a boutique private investment firm. His interest in optimal trade-sizing and risk-taking arose from each of these experiences and has culminated in the way Elm Wealth advises and invests for clients today.

James is an avid rock climber, classical guitarist, cook, and lover of renaissance history and music. When not in Elm's office or visiting clients, he can usually be found out climbing, hiking, eating, or traveling somewhere that nicely incorporates all three.

## Praise for The Missing Billionaires

This is a marvelous book that importantly extends the literature on financial decision-making. The authors creatively weave together the essence of practical considerations with insightful academic theory. One of a small handful of books that is timeless and should be read and reread over a lifetime for enjoyment and substance.
-Gary P. Brinson, CFA, Author, and Founder of Brinson Partners

The missing billionaires in the book's title allude to the difficulty of keeping already-made fortunes. Believing that nobody should get rich twice, Victor and James arm investors with lessons galore, drawn from their long practitioner careers. Yet the core lessons come from academia, and this wonderful book gives the best shot for Expected Utility and lifecycle models to finally become widely used in real-world investment decision-making. Uniquely, this book puts position sizing in the center, showing through many illustrations how "too much of a good thing" can be just too much.

> -Antti Ilmanen, Principal at AQR Capital, Author of Expected Returns

The Missing Billionaires addresses a topic that gets far too little attention in the investment community: how much to invest. The book is a terrific blend of theory, practice, and stories from the front lines. This is must-reading for anyone seeking to invest and spend wisely.
-Michael Mauboussin, Author and Head of Consilient Research, Morgan Stanley

I enjoyed and learned from Victor and James' book on incorporating uncertainty directly into making better financial decisions. Rightly so, for them, risk is front and center. This book is a great education for all of us, seamlessly marrying sophisticated theory with applications, demonstrating the beauty of a risk architecture that combines specificity with illuminating implementations into the lifetime wealth management problem.
-Myron S. Scholes, Frank E. Buck Professor of Finance, Emeritus, Stanford Graduate School of Business, Nobel Laureate in Economic Sciences

